

# QUIZ 1A

(CHAPTER 0: PRELIMINARY TOPICS)

MATH 141 – SPRING 2022 – KUNIYUKI

90 POINTS TOTAL

**No notes or books allowed. A scientific calculator is allowed. Simplify as appropriate.**

You may assume that two-dimensional graphs are in the usual Cartesian  $xy$ -plane (distances in meters). Give exact answers, unless you are told to approximate.

## SHORTER PROBLEMS (29 POINTS)

- 1) (1 point). The symbol  $\forall$  means which of the following? (Box in one.)  
For all                      There exists                      Is a member of
- 2) (6 points total).
  - a) Write the **converse** of this given statement:  
“If I finish ALEKS, then I get points.”
  - b) Write the **contrapositive** of this given statement:  
“If I finish ALEKS, then I get points.”
  - c) Which is logically equivalent to the given statement? (Box in one.)  
Its converse                      Its inverse                      Its contrapositive
- 3) (3 points). Give the piecewise definition of  $|a|$  (where  $a \in \mathbb{R}$ ) given in class.
- 4) (2 points). Mathematically express the following as an absolute value inequality: The distance between  $x$  and 5 on the real number line is less than 7.
- 5) (4 points). Solve the absolute value inequality from Problem 4); that is, solve the correct answer to Problem 4). Write the solution set in interval form (the form with parentheses and/or brackets).
- 6) (1 point). A student says that the expression  $(3a + 3b)^2$  is equivalent to  $3(a + b)^2$ . Is the student correct? Box in one:    Yes    No

7) (4 points). Write an equation for the line that passes through the point  $(4, 5)$  and that is perpendicular to the line  $y = \frac{7}{9}x - 10$ . Your answer may be in Point-Slope Form.

8) (8 points total; 2 points each). Write the formulas for the following.

Description	Formula
The <b>lateral surface area</b> of a right circular <b>cylinder</b> with base radius $r$ and height $h$	
The <b>volume</b> of a right circular <b>cylinder</b> with base radius $r$ and height $h$	
The <b>volume</b> of a right circular <b>cone</b> with base radius $r$ and height $h$	
The <b>surface area</b> of a <b>sphere</b> of radius $r$	

### LONGER PROBLEMS (61 POINTS)

Show all work, simplify as appropriate, and use “good form and procedure” (as in class).  
Box in your final answers!

9) (4 points). Simplify completely and fill in the box:  $\frac{(7^{2n})(7^{9n})}{(7^n)^3} = 7^{\boxed{\phantom{000}}}$

10) (6 points). Factor completely over  $\mathbb{Z}$  (that is, using only integer coefficients), as in class, and write as a fraction with no negative exponents:

$$3x^{-2} + x^{-3} - 2x^{-4}$$

11) (5 points). Simplify completely:  $\frac{2-x}{x^3-8}$

- 12) (4 points). Fill in the boxes below with real numbers in simplest form to make the statement correct.

$$\frac{7\sqrt{x} + 4}{x^2} = 7x \boxed{\phantom{00}} + 4x \boxed{\phantom{00}} \quad (x \neq 0)$$

- 13) Simplify the following expression completely, as in class.  
Your final answer must be a single non-compound fraction with no nonpositive exponents. (You do not have to rationalize denominators.)  
You may ignore domain issues here. (9 points)

$$\frac{x^4 \left( \frac{1}{2} \right) (2x+5)^{-1/2} (2) - (2x+5)^{1/2} (4x^3)}{(x^4)^2}$$

14) For parts a), b), and c) below, consider the points  $P(2, -1)$  and  $Q(6, 2)$  in the usual  $xy$ -plane. Write all numerical constants in simplest form. Distance is measured in meters. (19 points total)

a) Find the distance between the two points (that is, the length of the line segment  $\overline{PQ}$ ). (5 points)

b) Find the standard form of the equation of the circle that has  $P(2, -1)$  as its center and that passes through the point  $Q(6, 2)$  as a solution point. Hint: Part a) will help. (5 points)

c) Find the Slope-Intercept Form of the equation of the line  $\overleftrightarrow{PQ}$  that passes through the two points  $P$  and  $Q$ . This part can be done without parts a) and b). (9 points)

15) A spherical balloon has volume 300 cubic inches. Find the radius  $r$  of this balloon. Write an exact answer, and include appropriate units. (You do not have to rationalize denominators.) Also write an approximate answer in decimal form by rounding off to four significant digits. (8 points)

16)  $d$  is directly proportional to the cube of  $x$  and inversely proportional to  $t$ . Find the **particular** model equation related to this statement if  $d$  is 11 when  $x$  is 2 and  $t$  is 3, as in class. Make sure your model is in simplified form. (By “particular,” we mean determine the constant of proportionality.) (6 points)