

# MATH 150: OUTLINE FOR THE FINAL

## FUNCTIONS and TRIG (CHAPTER 1)

Finding the (implied) domain of a function  
Finding exact trig values  
Trig identities (Memorize and use Fundamental IDs and Advanced IDs;  
maybe use Product-to-Sum and Sum-to-Product IDs)  
Domains, ranges, and graphs of the six basic trig functions  
Simplifying trig expressions and verifying trig IDs  
Solving trig equations

## LIMITS AND CONTINUITY (CHAPTER 2)

Finding limits using basic properties and such tools as simple evaluation; sign analysis;  
limit forms; long-run limits involving  $\lim_{x \rightarrow \infty}$  or  $\lim_{x \rightarrow -\infty}$  : dividing by the highest  
power of (say)  $x$  in the denominator, short cuts for rational functions, dominant  
term substitution.  
One-sided vs. two-sided limits  
Knowing when a limit does not exist (DNE);  $\infty$  and  $-\infty$  are special cases  
Horizontal asymptotes (HAs) and long-run limits  
Vertical asymptotes (VAs) and infinite limits at a point  
0/0 indeterminate form:  
Tools include factoring and canceling/dividing, rationalizing; VAs vs. holes  
Squeeze (Sandwich) Theorem  
 $\varepsilon$ - $\delta$  definition of  $\lim_{x \rightarrow a} f(x) = L$   
Using  $\varepsilon$ - $\delta$  definitions to prove limit statements  $\leftarrow$  **not on the Final**  
Continuity  
Definition of continuity: at a point, on an open interval, on a closed interval  
Classifying discontinuities: removable, jump, infinite  
Where is  $f$  continuous / discontinuous?  
The Intermediate Value Theorem (IVT)

## DERIVATIVES (CHAPTER 3)

Rectilinear motion and projectile problems  
position  $s(t)$ , velocity  $v(t)$ , acceleration  $a(t)$   
Average rate of change on an interval vs. instantaneous rate of change  
The limit definition of derivative and its use in finding derivatives  
Tangent lines and their equations; derivatives as slopes of tangent lines  
Where is  $f$  differentiable / not differentiable? Also: corners, cusps, vertical tangent lines.  
Notation for derivatives  
Basic differentiation rules such as the linearity, product, quotient, power, and chain rules  
Finding  $D_x(\sin x)$  and  $D_x(\cos x)$  using the limit def'n of derivative  $\leftarrow$  **not on the Final**  
Finding the derivatives of other trig functions using the quotient or reciprocal rule  
Differentials and linear approximations to functions  
Implicit differentiation ("Imp Diff")  
Related rates  
If you get word problems on the Final, they will not involve elaborate setups.

## **APPLICATIONS OF DERIVATIVES (CHAPTER 4)**

Finding critical numbers (CNs) & corresponding points, PINs, and inflection points (IPs)  
The Extreme Value Theorem (EVT) and finding absolute maximum and minimum points for [the graph of] a function on a closed interval  
Rolle's Theorem and the Mean Value Theorem (MVT) for Derivatives  
Using the First and Second Derivative Tests to classify points at critical numbers (CNs) as local maximum points, local minimum points, or neither.  
Using the first derivative to see where  $f$  is increasing vs. decreasing  
Using the second derivative to see where the graph of  $f$  is concave up vs. concave down  
Optimization problems (see my comment under Related rates)  
Rectilinear motion and projectile problems  
Newton's Method for approximating roots (zeros) of  $f$

## **INTEGRALS (CHAPTER 5)**

Indefinite integrals (remember “ $+ C$ ” !!) vs. definite integrals (think “signed areas”)  
Solving differential equations subject to initial conditions, including physical applications  
Basic rules: linearity, power, trig  
 $u$ -substitutions  
    When evaluating definite integrals: Change the limits of integration immediately, or work out the corresponding indefinite integral first and then apply the FTC  
Using geometry to evaluate definite integrals  
Defining a definite integral as a limit of Riemann sums  
Properties of integrals  
The Mean Value Theorem (MVT) for Integrals,  $f_{av}$ : average value of  $f$  on an interval  
The Fundamental Theorem of Calculus (FTC), parts I and II  
    Part II is essential for evaluating definite integrals  
Numerical approximation of definite integrals  
    Left-hand, Right-hand, and Midpoint Riemann approximations using rectangles  
    Trapezoidal Rule and Simpson's Rule  $\leftarrow$  (formulas would be given)

## **APPLICATIONS OF INTEGRALS (CHAPTER 6)**

Finding areas (Tools include: Solving an equation for a variable, finding intersection points, which graph is on the top / bottom / right / left of a region, etc.)  
Finding volumes by using cross sections, including...  
    Finding volumes of solids of revolution using the Disk / Washer Method  
Finding volumes of solids of revolution using the Cylindrical Shells Method  
Arc length and surface areas of surfaces of revolution

## **LOGARITHMIC and EXPONENTIAL FUNCTIONS (CHAPTER 7)**

Defining  $\ln x$   
Differentiation and integration  
Logarithmic differentiation (“Log Diff”) and laws of logarithms  
Integrating  $\tan x$ ,  $\cot x$ ,  $\sec x$ ,  $\csc x$   
Working with  $e$  and bases other than  $e$

## **INVERSE TRIG FUNCTIONS and HYPERBOLIC FUNCTIONS (CHAPTER 8)**

See HW and HW Instructions for Chapter 8.